

CAMBRIDGE INTERNATIONAL EXAMINATIONS  
General Certificate of Education  
Advanced Subsidiary Level and Advanced Level

**MATHEMATICS**

**9709/01**

Paper 1 Pure Mathematics 1 **(P1)**

May/June 2003

**1 hour 45 minutes**

Additional materials: Answer Booklet/Paper  
Graph paper  
List of Formulae (MF9)

**READ THESE INSTRUCTIONS FIRST**

If you have been given an Answer Booklet, follow the instructions on the front cover of the Booklet.  
Write your Centre number, candidate number and name on all the work you hand in.  
Write in dark blue or black pen on both sides of the paper.  
You may use a soft pencil for any diagrams or graphs.  
Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer **all** the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.  
At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 75.

Questions carrying smaller numbers of marks are printed earlier in the paper, and questions carrying larger numbers of marks later in the paper.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

This document consists of **3** printed pages and **1** blank page.



1 Find the value of the coefficient of  $\frac{1}{x}$  in the expansion of  $\left(2x - \frac{1}{x}\right)^5$ . [3]

2 Find all the values of  $x$  in the interval  $0^\circ \leq x \leq 180^\circ$  which satisfy the equation  $\sin 3x + 2 \cos 3x = 0$ . [4]

3 (a) Differentiate  $4x + \frac{6}{x^2}$  with respect to  $x$ . [2]

(b) Find  $\int \left(4x + \frac{6}{x^2}\right) dx$ . [3]

4 In an arithmetic progression, the 1st term is  $-10$ , the 15th term is  $11$  and the last term is  $41$ . Find the sum of all the terms in the progression. [5]

5 The function  $f$  is defined by  $f : x \mapsto ax + b$ , for  $x \in \mathbb{R}$ , where  $a$  and  $b$  are constants. It is given that  $f(2) = 1$  and  $f(5) = 7$ .

(i) Find the values of  $a$  and  $b$ . [2]

(ii) Solve the equation  $ff(x) = 0$ . [3]

6 (i) Sketch the graph of the curve  $y = 3 \sin x$ , for  $-\pi \leq x \leq \pi$ . [2]

The straight line  $y = kx$ , where  $k$  is a constant, passes through the maximum point of this curve for  $-\pi \leq x \leq \pi$ .

(ii) Find the value of  $k$  in terms of  $\pi$ . [2]

(iii) State the coordinates of the other point, apart from the origin, where the line and the curve intersect. [1]

7 The line  $L_1$  has equation  $2x + y = 8$ . The line  $L_2$  passes through the point  $A(7, 4)$  and is perpendicular to  $L_1$ .

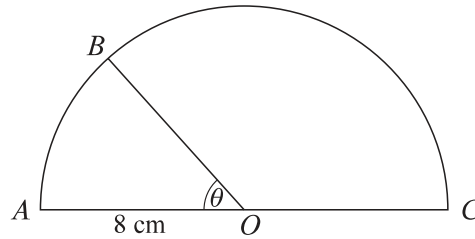
(i) Find the equation of  $L_2$ . [4]

(ii) Given that the lines  $L_1$  and  $L_2$  intersect at the point  $B$ , find the length of  $AB$ . [4]

8 The points  $A$ ,  $B$ ,  $C$  and  $D$  have position vectors  $3\mathbf{i} + 2\mathbf{k}$ ,  $2\mathbf{i} - 2\mathbf{j} + 5\mathbf{k}$ ,  $2\mathbf{j} + 7\mathbf{k}$  and  $-2\mathbf{i} + 10\mathbf{j} + 7\mathbf{k}$  respectively.

(i) Use a scalar product to show that  $BA$  and  $BC$  are perpendicular. [4]

(ii) Show that  $BC$  and  $AD$  are parallel and find the ratio of the length of  $BC$  to the length of  $AD$ . [4]



The diagram shows a semicircle  $ABC$  with centre  $O$  and radius 8 cm. Angle  $AOB = \theta$  radians.

- (i) In the case where  $\theta = 1$ , calculate the area of the sector  $BOC$ . [3]
- (ii) Find the value of  $\theta$  for which the perimeter of sector  $AOB$  is one half of the perimeter of sector  $BOC$ . [3]
- (iii) In the case where  $\theta = \frac{1}{3}\pi$ , show that the exact length of the perimeter of triangle  $ABC$  is  $(24 + 8\sqrt{3})$  cm. [3]

10 The equation of a curve is  $y = \sqrt{(5x + 4)}$ .

- (i) Calculate the gradient of the curve at the point where  $x = 1$ . [3]
- (ii) A point with coordinates  $(x, y)$  moves along the curve in such a way that the rate of increase of  $x$  has the constant value 0.03 units per second. Find the rate of increase of  $y$  at the instant when  $x = 1$ . [2]
- (iii) Find the area enclosed by the curve, the  $x$ -axis, the  $y$ -axis and the line  $x = 1$ . [5]

11 The equation of a curve is  $y = 8x - x^2$ .

- (i) Express  $8x - x^2$  in the form  $a - (x + b)^2$ , stating the numerical values of  $a$  and  $b$ . [3]
- (ii) Hence, or otherwise, find the coordinates of the stationary point of the curve. [2]
- (iii) Find the set of values of  $x$  for which  $y \geq -20$ . [3]

The function  $g$  is defined by  $g : x \mapsto 8x - x^2$ , for  $x \geq 4$ .

- (iv) State the domain and range of  $g^{-1}$ . [2]
- (v) Find an expression, in terms of  $x$ , for  $g^{-1}(x)$ . [3]

